Hadronic Matrix Elements & EDMs



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Lattice Meets Experiment Workshop BNL, December 2013

Outline

- I. Introduction: Motivation & Experimental Situation
- II. Interpreting EDMs
- III. EDMs in Strongly Interacting Systems
- IV. Hadronic Matrix Elements: The Challenge
- V. Implications & Outlook

I. Introduction

Why are EDMs Interesting?

- Does QCD violate CP?
- What is the BSM CPV needed for baryogenesis?
- What is the BSM mass scale?

EDM Experiments



PHYSICAL REVIEW

VOLUME 108, NUMBER 1

OCTOBER 1, 1957

Experimental Limit to the Electric Dipole Moment of the Neutron

J. H. SMITH,* E. M. PURCELL, AND N. F. RAMSEY

Oak Ridge National Laboratory, Oak Ridge, Tennessee, and Harvard University, Cambridge, Massachusetts

(Received May 17, 1957)

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EDM Experiments



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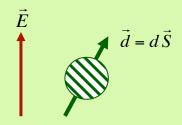
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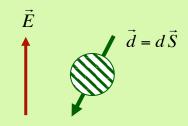
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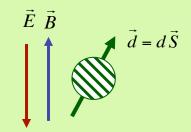


$$v_{EDM} = -\frac{d\vec{S} \cdot \vec{E}}{h}$$



$$v_{EDM} = -\frac{d(-\vec{S}) \cdot \vec{E}}{h}$$

T-odd → CPodd by CPT theorem



$$v_{EDM} = -\frac{dS \cdot (-E)}{h}$$

P-odd: used to find signal

EDMs: New CPV?

System	Limit (e cm)*	SM CKM CPV	BSM CPV
¹⁹⁹ Hg	3.1 x 10 ⁻²⁹	10 ⁻³³	10 ⁻²⁹
d _e (ThO)	8.7 x 10 ⁻²⁹ **	10 -38	10 ⁻²⁹
n	3.3 x 10 ⁻²⁶	10 ⁻³¹	10 ⁻²⁶

^{* 95%} CL ** 90% CL, no eq CPV

(thanks: T. Chupp)

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Mass Scale Sensitivity

$$\psi$$
 ϕ $\sin\phi_{CP} \sim 1 o M > 5000 \ {
m GeV}$ ϕ $M < 500 \ {
m GeV} o \sin\phi_{CP} < 10^{-2}$

$$sin\phi_{CP} \sim 1 \rightarrow M > 5000 \text{ GeV}$$

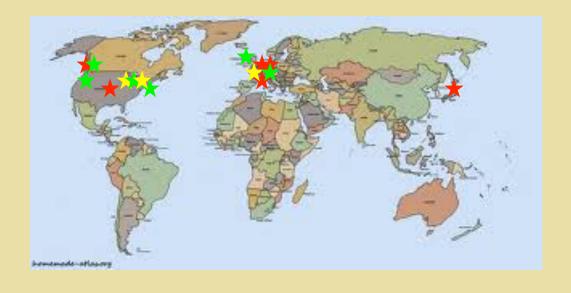
$$M$$
 < 500 GeV $ightarrow$ sin ϕ_{CP} < 10-2

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(thanks: T. Chupp)



neutron

proton & nuclei

atoms

~ 100 x better sensitivity

Not shown: muon

II. Interpreting EDMs

Why Multiple Systems?

Why Multiple Systems?

Multiple sources & multiple scales

EDM Interpretation & Multiple Scales Collider Searches Baryon Asymmetry Particle spectrum; also **BSM CPV Early universe CPV** scalars for baryon asym SUSY, GUTs, Extra Dim... Energy Scale **QCD Matrix Elements Nuclear & atomic MEs** Schiff moment, other P- & d_n , $g_{\pi NN}$, ... T-odd moments, e-nucleus **Expt CPV** 13

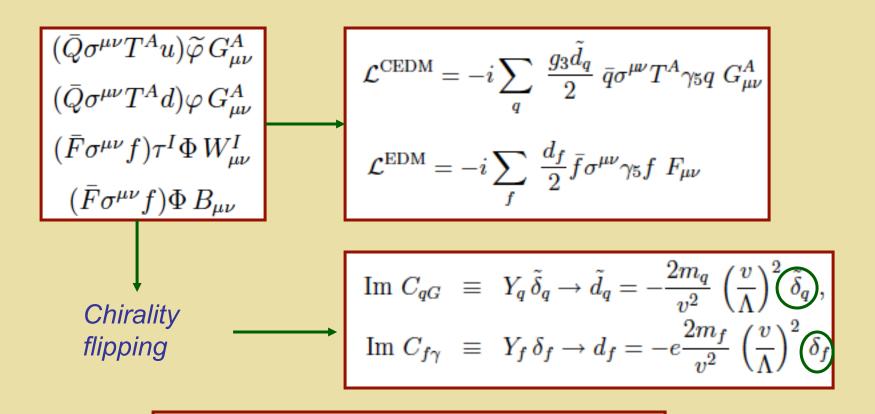
Effective Operators

$$\mathcal{L}_{\mathrm{CPV}} = \mathcal{L}_{\mathrm{CKM}} + \mathcal{L}_{ar{ heta}} + \mathcal{L}_{\mathrm{BSM}}^{\mathrm{eff}}$$

$$\mathcal{L}_{\mathrm{BSM}}^{\mathrm{eff}} = \frac{1}{\Lambda^2} \sum_{i} \alpha_i^{(n)} O_i^{(6)} + \dots$$

EDM Interpretation & Multiple Scales **Collider Searches Baryon Asymmetry BSM CPV** Particle spectrum; also **Early universe CPV** scalars for baryon asym SUSY, GUTs, Extra Dim... Energy Scale d= 6 Effective Operators: "CPV Sources" fermion EDM, quark chromo EDM, 3 gluon, 4 fermion **QCD Matrix Elements Nuclear & atomic MEs** Schiff moment, other P- & d_n , $g_{\pi NN}$, ... T-odd moments, e-nucleus **Expt CPV** 15

Wilson Coefficients: EDM & CEDM



 δ_f , δ_q appropriate for comparison with other d=6 Wilson coefficients

Wilson Coefficients: Summary

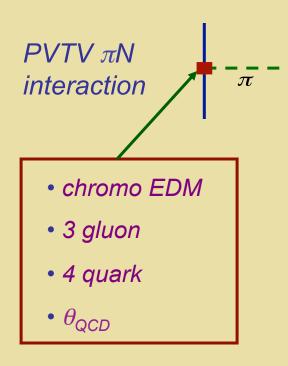
$\delta_{\!f}$	fermion EDM	(3)
$oldsymbol{\widetilde{\delta}}_q$	quark CEDM	(2)
C̃ _G	3 gluon	(1)
C _{quqd}	non-leptonic	(2)
C _{lequ, ledq}	semi-leptonic	(3)
$C_{arphi ud}$	induced 4f	(1)

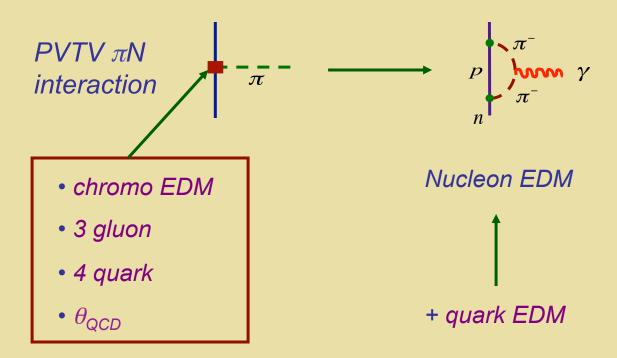
12 total +
$$\overline{\theta}$$

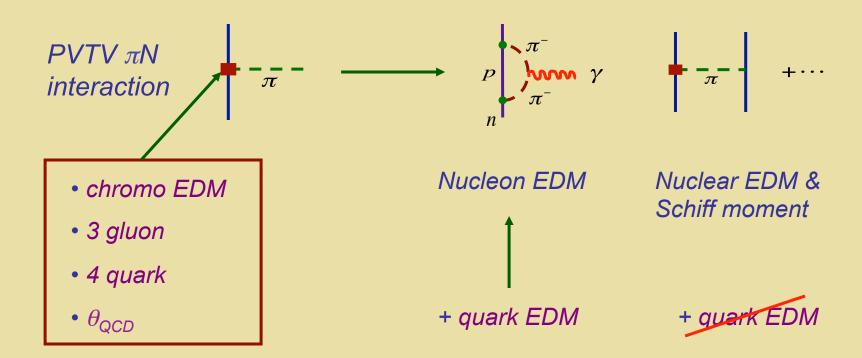
light flavors only (e,u,d)

III. EDMs of Strongly Interacting Systems

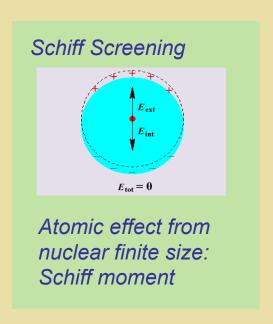






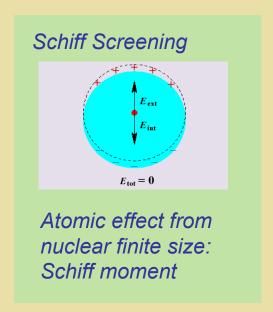


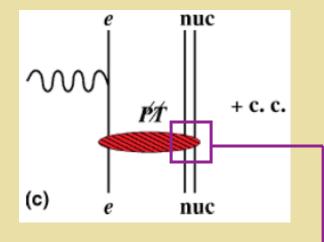
Diamagnetic Systems: Schiff Moments



Neutral atoms: nuclear EDM invisible to external probe

Diamagnetic Systems: Schiff Moments





Schiff moment, MQM,...

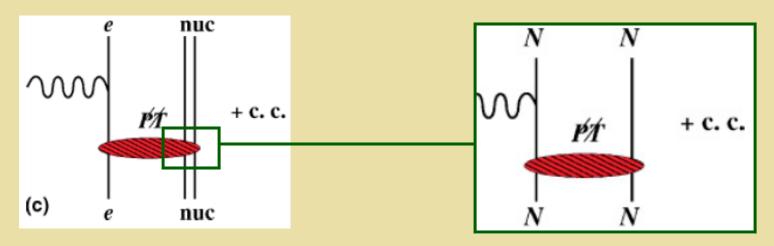
Nuclear Schiff Moment

$$S \sim \int d^3x \ x^2 \ \vec{x} \ \rho(\vec{x})^{CPV}$$

 $(R_N/R_A)^2$ suppression

Nuclear Schiff Moment

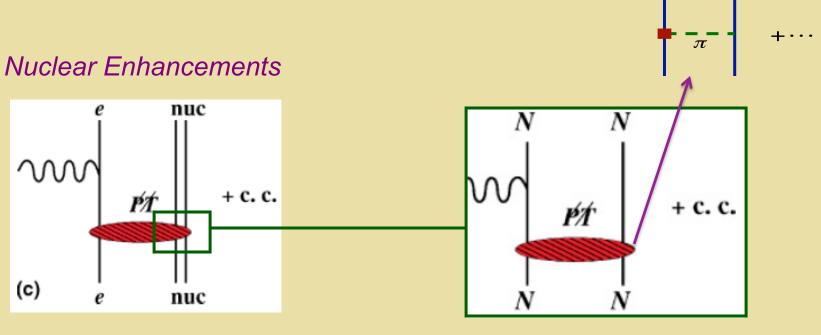
Nuclear Enhancements



Schiff moment, MQM,...

Nuclear polarization: mixing of opposite parity states by $H^{TVPV} \sim 1 / \Delta E$

Nuclear Schiff Moment



Schiff moment, MQM,...

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IV. Hadronic Matrix Elements: Challenges

d_N "Short distance" nucleon EDM

 $\overline{g_{\pi}}^{(i)}$ TVPV π NN couplings: i=0,1,2

$$d_n = \bar{d}_n - \frac{eg_A}{4\pi^2 F_\pi} \left\{ \bar{g}_\pi^{(0)} \left(\ln \frac{m_\pi^2}{m_N^2} - \frac{\pi m_\pi}{2m_N} \right) + \frac{\bar{g}_\pi^{(1)}}{4} \left(\kappa_1 - \kappa_0 \right) \frac{m_\pi^2}{m_N^2} \ln \frac{m_\pi^2}{m_N^2} \right\} \right\}$$

Running & Matching Hadronic

$$d_N = \alpha_N \,\bar{\theta} + \left(\frac{v}{\Lambda}\right)^2 \,\sum_k \beta_N^{(k)} \,(\operatorname{Im} C_k)$$

$$\bar{g}_{\pi}^{(i)} = \lambda_{(i)} \,\bar{\theta} + \left(\frac{v}{\Lambda}\right)^2 \,\sum_k \gamma_{(i)}^{(k)} \,(\operatorname{Im} C_k)$$

$$\left(\frac{v}{\Lambda}\right)^2 \left[\beta_N^{qG} \left(\operatorname{Im} C_{qG}\right) + \beta_N^{q\gamma} \left(\operatorname{Im} C_{q\gamma}\right)\right] = e \,\tilde{\rho}_N^q \,\tilde{d}_q + \rho_N^q \,d_q = \left(\frac{v}{\Lambda}\right)^2 \left[e \,\tilde{\zeta}_N^q \,\tilde{\delta}_q + e \,\zeta_N^q \,\delta_q\right]$$

$$\left(\frac{v}{\Lambda}\right)^2 \left[\gamma_{(i)}^{qG} \left(\operatorname{Im} C_{qG}\right) + \gamma_{(i)}^{q\gamma} \left(\operatorname{Im} C_{q\gamma}\right)\right] = \tilde{\omega}_{(i)}^q \,\tilde{d}_q + \omega_{(i)}^q \,d_q = \left(\frac{v}{\Lambda}\right)^2 \left[\tilde{\eta}_{(i)}^q \,\tilde{\delta}_q + \eta_{(i)}^q \,\delta_q\right]$$

How well can we compute the β , ρ , ζ , ... ?

Hadronic Matrix Elements: Approaches

- Chiral symmetry & NDA
- Lattice
- QCD Sum Rules
- Dyson Schwinger Equations
- Quark Models

•

Param	Coeff	Best value ^a	Range
$\bar{ heta}$	$lpha_n$ $lpha_p$	0.002 0.002	(0.0005-0.004) (0.0005-0.004)
Im C _{qG}	$eta_n^{uG} eta_n^{dG}$	4×10^{-4} 8×10^{-4}	$(1-10) \times 10^{-4}$ $(2-18) \times 10^{-4}$
$ ilde{d}_q$	$e ilde{ ho}^u_n \ e ilde{ ho}^d_n$	-0.35 -0.7	-(0.09 - 0.9) -(0.2 - 1.8)
$ ilde{\delta}_q$	$e\tilde{\zeta}_n^u$ $e\tilde{\zeta}_n^d$	8.2×10^{-9} 16.3×10^{-9}	$(2-20) \times 10^{-9}$ $(4-40) \times 10^{-9}$
Im C _{qy}	$eta_{n}^{u\gamma} \ eta_{n}^{d\gamma}$	0.4×10^{-3} -1.6×10^{-3}	$(0.2 - 0.6) \times 10^{-3}$ $-(0.8 - 2.4) \times 10^{-3}$
d_q	$ ho_n^u ho_n^d$	-0.35 1.4	(-0.17)-0.52 0.7-2.1
δ_q	ζ ^u ζ ^d ζ ⁿ	8.2×10^{-9} -33×10^{-9}	$(4-12) \times 10^{-9}$ - $(16-50) \times 10^{-9}$
C _G	$oldsymbol{eta}_n^{ ilde{G}}$	2×10^{-7}	$(0.2-40) \times 10^{-7}$
$\operatorname{Im} C_{\varphi ud}$	$oldsymbol{eta}_{n}^{arphi ud}$	3×10^{-8}	$(1-10) \times 10^{-8}$
$\operatorname{Im} C_{quqd}^{(1,8)}$	$oldsymbol{eta}_n^{quqd}$	40×10^{-7}	$(10-80) \times 10^{-7}$
$\operatorname{Im} C_{eq}^{(-)}$	$g_{\rm S}^{(0)}$	12.7	11-14.5
Im C _{eq} ⁽⁺⁾	g _S ⁽¹⁾	0.9	0.6-1.2

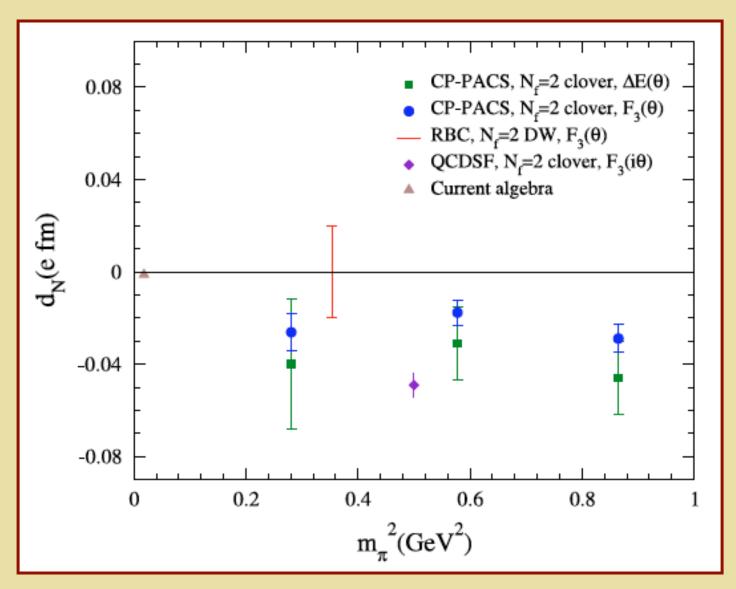
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Hadronic Matrix Elements: θ_{QCD}

Chiral symmetry & NDA

$$\bar{g}_{\pi}^{(0)} = \frac{1 - \epsilon^2}{2\epsilon} \frac{(\Delta m_N)_q}{F_{\pi}} \bar{\theta} \longrightarrow \lambda_{(0)} = \frac{1 - \epsilon^2}{2\epsilon} \frac{(\Delta m_N)_q}{F_{\pi}}$$

$$ar{d}_{0,1} \sim ear{ heta} \; rac{m_\pi^2}{\Lambda_\chi^3} \qquad \longrightarrow \qquad lpha_N \sim e \, rac{m_\pi^2}{\Lambda_\chi^3} \sim 0.2 \, rac{m_\pi^2}{\Lambda_\chi^2} \, e \, \mathrm{fm}$$



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ρ EDM

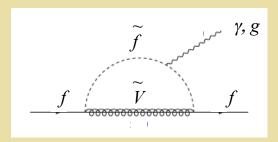
$q\gamma q$	$-0.066 ilde{d}_{-}^{e}-0.199 ilde{d}_{+}^{e}$
BSA	$-0.120 ilde{d}_{-}^{e}+0.108 ilde{d}_{+}^{e}$
S(k)	$1.538 ilde{d}^e$
acm $(\times \mu^{\text{acm}})$	$0.775 ilde{d}_{-}^{e} + 2.396 ilde{d}_{+}^{e}$
$our\ CEDM$	$(1.35 + 0.78 \mu^{\text{acm}}) \tilde{d}_{-}^{e} - (0.09 - 2.40 \mu^{\text{acm}}) \tilde{d}_{+}^{e}$
total	$1.16 ilde{d}_{-}^{e} - 0.69 ilde{d}_{+}^{e}$
sum rules [15]	$-0.13 ilde{d}^e$

DSE: Pitschmann et al, 1209.4352,

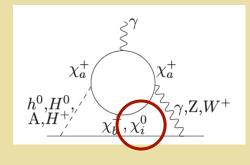
PRC 87 (2013) 015205

V. Implications & Outlook

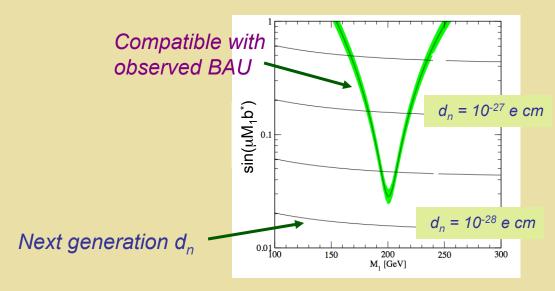
EDMs & EW Baryogenesis: MSSM



Heavy sfermions: LHC consistent & suppress 1-loop EDMs

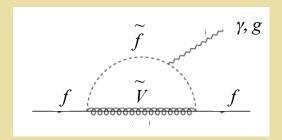


Sub-TeV EW-inos: LHC & EWB - viable but non-universal phases

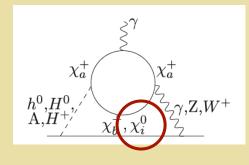


Li, Profumo, RM '09-'10

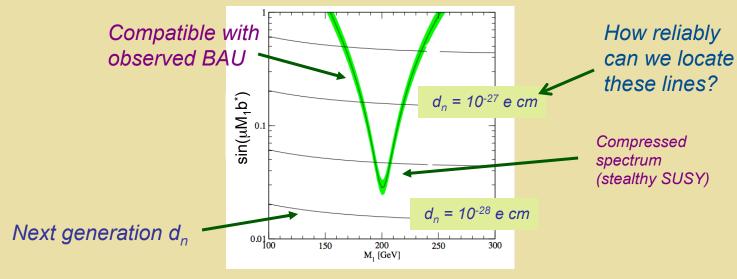
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Li, Profumo, RM '09-'10

V. Implications & Outlook

- EDMs provide a powerful probe of CPV physics at the multi-TeV scale
- Searches in a variety of systems needed to uncover and disentangle effects associated with different "sources" (eg, d=6 operators)
- Obtaining reliable non-perturbative computations remains a key open challenge, with implications for interpretation of EDMs in terms of BSM physics & cosmology

Back Up Slides

 δ_f MSSM, RS, LRSM 1 & 2 loop

 $\widetilde{\delta}_a$ MSSM, RS, LRSM 1 & 2 loop

 $C_{\widetilde{G}}$ MSSM 2 loop

 C_{auad} (MSSM d=8)

 $C_{leau, leda}$ (MSSM d=8)

 $C_{\varphi ud}$ LRSM tree (θ_{LR})

12 total + $\overline{\theta}$

light flavors only (e,u,d)

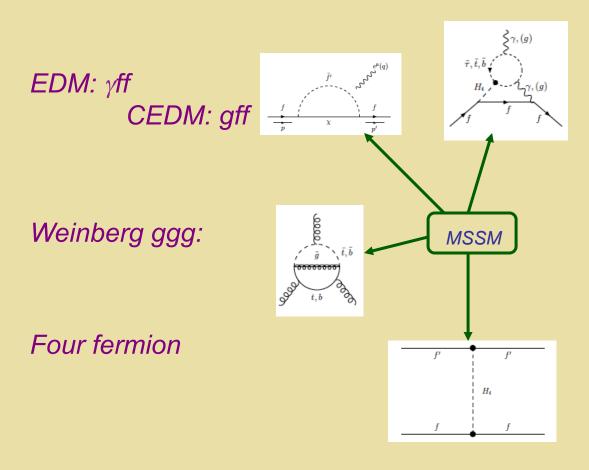
EDM: γff

CEDM: gff

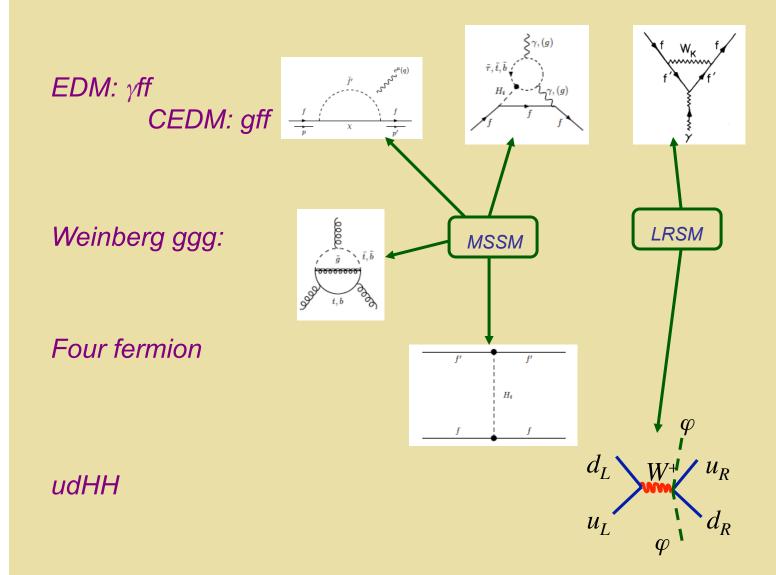
Weinberg ggg:

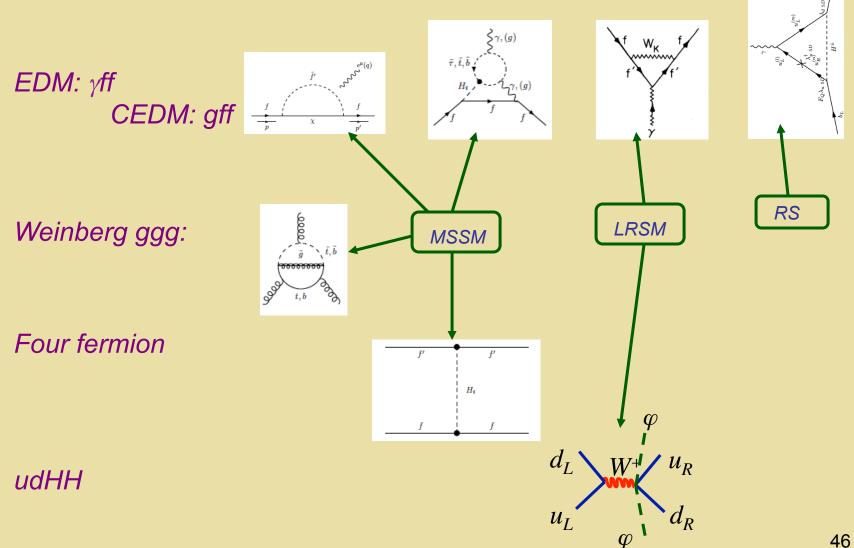
Four fermion

udHH



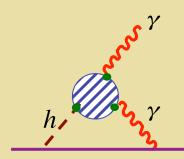
udHH

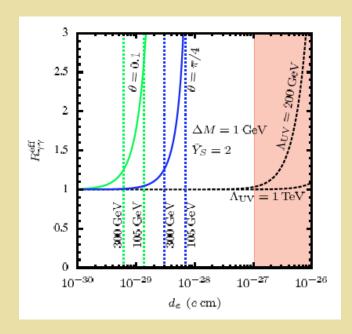




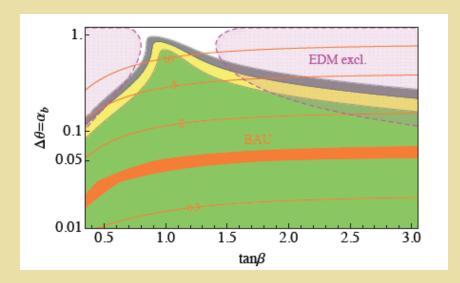
Recent Interest: EDMs & $H \rightarrow \gamma \gamma$

$$\frac{c_h v}{\Lambda^2} h F_{\mu\nu} F^{\mu\nu} + \frac{\tilde{c}_h v}{\tilde{\Lambda}^2} h F_{\mu\nu} \tilde{F}^{\mu\nu}$$





McKeen, Pospelov, Ritz '12 SM + singlet & vector-like leptons



Shu, Zhang '13
2HDM & connection with BAU

Diamagnetic Systems

Nuclear Moments

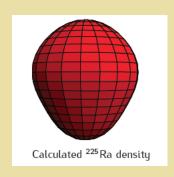
Diamagnetic Systems

Nuclear Moments



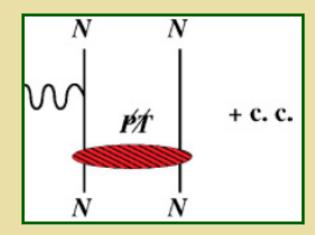
Nuclear Schiff Moment

Nuclear Enhancements: Octupole Deformation



$$|\pm\rangle = \frac{1}{\sqrt{2}} (| \bigcirc \rangle \pm | \bigcirc \rangle)$$

Opposite parity states mixed by H^{TVPV}



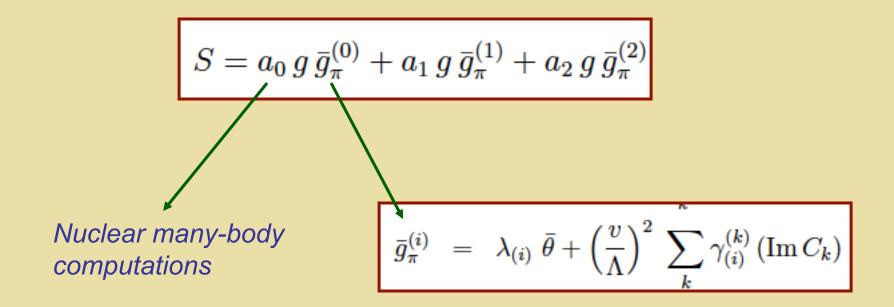
Nuclear polarization: mixing of opposite parity states by $H^{TVPV} \sim 1 / \Delta E$

"Nuclear amplifier"

EDMs of diamagnetic atoms (²²⁵Ra)

Running & Matching

Nuclear

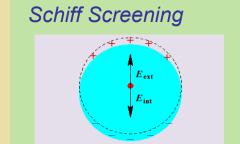


Non-perturbative hadronic computations

Nuclear Matrix Elements

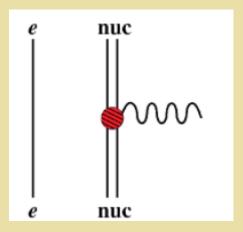
Nucl.	Best value		
	<i>a</i> ₀	a_1	a_2
¹⁹⁹ Hg ¹²⁹ Xe ²²⁵ Ra	0.01 -0.008 -1.5	± 0.02 -0.006 6.0	0.02 -0.009 -4.0
Range			
a_0	a_1		a_2
0.005-0.05 -0.005-(-0.05) -1-(-6)	-0.03-(+0.09) -0.003-(-0.05) 4-24		0.01-0.06 -0.005-(-0.1) -3-(-15)

Schiff Screening & Corrections

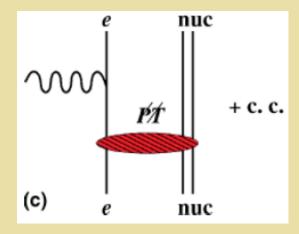


 $E_{\text{tot}} = 0$

Atomic effect from nuclear finite size: Schiff moment



Screened EDM



Schiff moment, MQM,...

EDM, Schiff...

MQM....

$$T^{E}_{J=1} \otimes T^{E}_{J=2}$$
 ?

EDMs of diamagnetic atoms (199Hg)